

B.L.D.E.A's
S.B. ARTS AND K.C.P. SCIENCE COLLEGE, VIJAYAPUR-586 103
DEPARTMENT OF MATHEMATICS
First Internal Assessment

Sem: I Sub: Algebra-I and Calculus-I (DSC1) Code: 21BSC1C1MAT1L

Date: 05 - 01 - 2024 Time: 1:30 PM - 2:30 PM Max. Marks: 30

Q.No.1. Answer Any Three Questions

2×3=6

- a) Find the rank of a matrix $A = \begin{bmatrix} 2 & 1 & -1 \\ 0 & 3 & -2 \\ 2 & 4 & -3 \end{bmatrix}$.
- b) If φ for the curve $r = ae^{b\theta}$.
- c) If $f(x) = \begin{cases} \frac{x}{|x|} & \text{when } x \neq 0 \\ 0 & \text{when } x = 0 \end{cases}$, then show that $f(x)$ is discontinuous at $x=0$.
- d) Find the n^{th} derivative of e^{ax+b} .

Q.No.2. Answer Any Three Questions

4×3=12

- a) Verify the Cayley-Hamilton theorem for the matrix $A = \begin{bmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 2 & 0 & 3 \end{bmatrix}$ and

hence find A^{-1} .

- b) Write a matrix $\begin{bmatrix} 1 & 2 & 4 \\ -1 & 5 & 3 \\ -1 & 6 & 3 \end{bmatrix}$ as the sum of symmetric and skew symmetric

matrix.

- c) Derive the expression for angle between the radius vector and tangent at any point on the curve.
- d) Find the pedal equation of the curve $r = a(1 - \cos\theta)$.

Q.No.3. Answer Any Three Questions

4×3=12

- a) If $\lim_{x \rightarrow a} f(x) = l$ and $\lim_{x \rightarrow a} g(x) = m$, then prove that $\lim_{x \rightarrow a} [f(x) * g(x)] = l * m$.
- b) If a function $f(x)$ is continuous in $[a, b]$, then show that it is bounded in $[a, b]$.
- c) State and prove Leibnitz's theorem.
- d) Find the n^{th} derivative of $\frac{x}{(x-a)(x-b)}$.

B.L.D.E.A's
S.B. ARTS AND K.C.P. SCIENCE COLLEGE, VIJAYAPUR-586 103
DEPARTMENT OF MATHEMATICS

First Internal Assessment

Sem: III

Sub: Ordinary Differential Equations and
Real Analysis - I (DSC)

Code: 21BSC3C3MAT1L

Date-03-01-2024

Time: 1:30 PM - 2:30 PM

Max. Marks: 30

Q.No.1. Answer Any Three Questions

2×3=6

- a) Solve $(4x + 3y + 1)dx + (3x + 2y + 1)dy = 0$.
- b) Solve $(D^2 - 9)y = 0$.
- c) Define oscillatory sequence. With an example.
- d) Show that the series $1^2 + 2^2 + 3^2 + \dots + n^2 + \dots$ diverges to $+\infty$.

Q.No.2. Answer Any Three Questions

4×3=12

- a) State and prove necessary and sufficient condition for the equation to be exact.
- b) Solve $(3x^2 + 6xy^2)dx + (6x^2y + 4y^3)dy = 0$.
- c) With usual notation prove that $\frac{1}{f(D)}e^{ax} = \frac{1}{f(a)}e^{ax}$, if $f(a) \neq 0$.
- d) Solve $(D^3 + D^2 + 4D + 4)y = 0$.

Q.No.3. Answer Any Three Questions

4×3=12

- a) If $\lim_{n \rightarrow \infty} a_n = a, \lim_{n \rightarrow \infty} b_n = b$ then prove that $\lim_{n \rightarrow \infty} a_n + b_n = a + b$.
- b) If $\lim_{n \rightarrow \infty} a_n = l, \lim_{n \rightarrow \infty} b_n = m$ then prove that $\lim_{n \rightarrow \infty} (a_n b_n) = lm$.
- c) State and prove p-series test.
- d) Test the convergence $\frac{1}{3.7} + \frac{1}{4.9} + \frac{1}{5.11} + \frac{1}{6.13}$

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S.B. ARTS AND K.C.P. SCIENCE COLLEGE, VIJAYAPUR-586 103
DEPARTMENT OF MATHEMATICS

First Internal Assessment

Sem: III

**Sub: Ordinary Differential Equations
(OEC)**

Code: 21BSC303MAT3-A

Date: 06 - 01 - 2024

Time: 1:30 PM - 2:30 PM

Max. Marks: 30

Q.No.1. Answer Any Three Questions

2×3=6

- a) Define Ordinary Differential Equation.
- b) Solve $p^2 - 5p - 6 = 0$.
- c) Solve $p^2 + p = 6$.
- d) Solve $(D^2 - 4)y = 0$

Q.No.2. Answer Any Two Questions

4×2=8

- a) State and prove Necessary condition for exact differential equation.
- b) Solve $(3x^2 + 6xy^2)dx + (6x^2y + 4y^3)dy$.
- c) Solve $(e^y + 1) \cos x dx + e^y \sin x dy = 0$.

Q.No.3. Answer Any Two Questions

4×2=8

- a) Solve $p^2 + p(x + y) + xy = 0$.
- b) Solve $x^2p^2 = 6y^2$.
- c) Solve $yp^2 - (1 + xy)p + x = 0$.

Q.No.3. Answer Any Two Questions

4×2=8

- a) Solve $(D^3 + D^2 + 4D + 4)y = 0$
- b) Solve $(D^3 - 6D^2 + 11D - 6)y = 0$
- c) With usual notation prove that $\frac{1}{f(D)} e^{ax} = \frac{1}{f(a)} e^{ax}$, if $f(a) \neq 0$

B.L.D.E.A's
S.B. ARTS AND K.C.P. SCIENCE COLLEGE, VIJAYAPUR-586 103
DEPARTMENT OF MATHEMATICS
First Internal Assessment Jan-2024

Sem: V Sub: Real Analysis – II and Complex Analysis Code: 21BSC5C5MATMJ1L

Date: 04 – 01 – 2024

Time: 3:00 PM – 4:00 PM

Max. Marks: 30

Q.No.1. Answer any three of the following.

2×3=6

- a) Define upper and lower Riemann sum.
- b) Find the convergence of $\int_1^{\infty} \frac{dx}{x^{3/2}}$.
- c) Check whether the given function $f(z) = x^2 + y^2 + ixy$ is analytic or not.
- d) State Cauchy's integral theorem and evaluate $\oint_C \frac{dz}{z-a}$ where C is the circle $|z - a| = r$.

Q.No.2. Answer any three of the following.

4×3=12

- a) Find $L(P, f)$ and $U(P, f)$ for the function defined by $f(x) = x^2$ on $[0, 1]$ and $P = \{0, \frac{1}{4}, \frac{2}{4}, \frac{3}{4}, 1\}$.
- b) State and prove necessary and sufficient condition for R-integrability.
- c) The improper integral $\int_a^b \frac{dx}{(x-a)^n}$ is convergent if $n < 1$, divergent if $n \geq 1$.
- d) Test the convergence of $\int_0^1 \frac{dx}{\sqrt{x^2+x}}$.

Q.No.3. Answer any three of the following.

4×3=12

- a) Find the harmonic conjugate of $u = \cos x \cosh y$ and also show that u is harmonic.
- b) State and prove necessary condition for a function to be analytic.
- c) State and prove Cauchy's integral formula.
- d) Evaluate $\oint_C \frac{z-1}{(z+1)(z-2)} dz$ where $C: |z - i| = 2$.

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DEPARTMENT OF MATHEMATICS
First Internal Assessment Jan-2024

Sem: V

Sub: Vector Integration and Analytical
Geometry

Code: 21BSC5C5MATMJ2L

Date: 05 - 01 - 2024

Time: 12:00 Noon - 1:00 PM

Max. Marks: 30

Q.No.1. Answer any three of the following.

2×3=6

- a) Define derivative of a vector function.
- b) Define vector line integral.
- c) Define sphere and write the different forms of sphere.
- d) Define Cone.

Q.No.2. Answer any three of the following.

4×3=12

- a) If $\vec{A}(t)$ and $\vec{B}(t)$ are two differential vector functions of a scalar variable t , then prove that $\frac{d}{dt} \{ \vec{A}(t) \cdot \vec{B}(t) \} = \vec{A}(t) \cdot \frac{d}{dt} \vec{B}(t) + \vec{B}(t) \cdot \frac{d}{dt} \vec{A}(t)$.
- b) Prove that the necessary and sufficient condition for $\vec{f}(t)$ to be constant $\frac{d\vec{f}}{dt} = 0$.
- c) State and prove Green's theorem in the plane.
- d) Verify Green's theorem in the plane for $\oint_C (xy + y^2)dx + x^2dy$ where C is the closed curve made up of $y = x$ and $y = x^2$.

Q.No.3. Answer any three of the following.

4×3=12

- a) Prove that the equation $ax^2 + ay^2 + az^2 + 2ux + 2vy + 2wz + d = 0$ represents a sphere and find its center and radius.
- b) Show that the spheres $x^2 + y^2 + z^2 = 25$ and $x^2 + y^2 + z^2 - 18x - 24y - 4z + 225 = 0$ touch externally and find the co-ordinates of their common point.
- c) Find the equation of cone with vertex at the origin is homogenous in x, y, z of the type
 $ax^2 + by^2 + cz^2 + 2fyz + 2gzx + 2hxy + ux_1 + vy_1 + wz_1 + d = 0$
- d) Find the equation of the cone given vertex $v(1,1,3)$ which passes through ellipse $4x^2 + z^2 = 1$ and $y = 4$.

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Second Internal Assessment

Sem: I

Sub: Algebra-I and Calculus-I (DSC1)

Code: 21BSC1C1MAT1L

Date: 13 - 02-2024

Time: 1:30 PM - 2:30 PM

Max. Marks: 30

Q.No.1. Answer Any Three Questions

2×3=6

- a) Write any four properties of eigen values of square matrix.
- b) If φ for the curve $r^2 \cos 2\theta = a^2$.
- c) State Rolle's Theorem.
- d) Find the n^{th} derivative of $\log x^2 - 4x + 4$.

Q.No.2. Answer Any Three Questions

4×3=12

- a) Find the inverse of the matrix by elementary transformation

$$A = \begin{bmatrix} 1 & 2 & 1 \\ 3 & 2 & 3 \\ 1 & 1 & 2 \end{bmatrix}$$

- b) Solve the system of equation by elementary transformation
 $3x + y + 2z = 3, 2x - 3y - z = -3, x + 2y + z = 4$.
- c) Derivatives of Arc in Cartesian form .
- d) Show that the pedal equation of the circle $x^2 + y^2 = 2ax$.

Q.No.3. Answer Any Three Questions

4×3=12

- a) State and Prove Cauchy's Mean Value Theorem.
- b) Verify Rolle's theorem for $f(x) = x^2 - 6x + 8$ in $[2, 4]$.
- c) Find the n^{th} derivative of $\sin x * \sin 2x * \sin 3x$.
- d) If $y = \sin (m \sin^{-1} x)$, then S.T

$$(1 - x^2)y_{n+2} - (2n + 1)xy_{n+1} + (m^2 - n^2)y_n = 0.$$

Sem: III

Sub: Ordinary Differential Equations and
Real Analysis - I(DSC)

Code: 21BSC3C3MAT1L

Date-10-02-2024

Time: 1:30 PM - 2:30 PM

Max. Marks: 30

Q.No.1. Answer Any Three Questions

2×3=6

- a) Solve $p^2 - 5p - 6 = 0$.
- b) Find the complimentary function of $(D^2 - 2D + 1)y = \cos 3x$.
- c) Prove that the sequence $\left\{\frac{n}{n+1}\right\}$ is monotonic increasing sequence.
- d) State Raabe's test.

Q.No.2. Answer Any Three Questions

4×3=12

- a) Solve $(x^2y - 2xy^2)dx - (x^3 - 3x^2y)dy = 0$.
- b) Solve $p^2 + p(x + y) + xy = 0$.
- c) Derive the condition for integrability of total differential equation $Pdx + Qdy + Rdz = 0$.
- d) Solve $(D^2 + 1)y = x \sin 2x$.

Q.No.3. Answer Any Three Questions

4×3=12

- a) State and prove cauchys second theorem on limits.
- b) Prove that the sequence $\{a_n\}$ where $a_n = \frac{1}{n+1} + \frac{1}{n+2} + \frac{1}{n+3} + \dots + \frac{1}{2n}$ is convergent and its limit lies between $\frac{1}{2}$ and 1
- c) State and prove D'Alembert's test.
- d) Test the convergence $\frac{1}{2\sqrt{1}} + \frac{x^2}{3\sqrt{2}} + \frac{x^4}{4\sqrt{3}} + \frac{x^6}{5\sqrt{4}} \dots$



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Second Internal Assessment

Sem: III

**Sub: Ordinary Differential Equations
(OEC)**

Code: 21BSC303MAT3-A

Date: 13-02-2023

Time: 12:00 PM - 1:00 PM

Max. Marks: 30

Q.No.1. Answer Any Three Questions

2×3=6

- a) Solve $(D^2 + 1)y = 1$.
- b) Define differential equation. What are the types of differential equation.
- c) Define Exact differential equation.
- d) Define Singular solution.

Q.No.2. Answer Any Two Questions

4×2=8

- a) Solve $(D^2 + 4)y = \sin 2x + e^x$.
- b) Solve $(D^2 + 2D + 1)y = x \cos x$.
- c) Solve $(D^2 - 3D + 2)y = x^2 e^{3x}$.

Q.No.3. Answer Any Two Questions

4×2=8

- a) Solve $(xy^2 + 2x^2y^3)dx + (x^2y + x^3y^2)dy = 0$.
- b) Solve $(3xy - 2ay^2)dx + (x^2 - 2ayx)dy = 0$.
- c) Solve $(x^2 + y^2 + 2x)dx + 2ydy = 0$.

Q.No.4. Answer Any Two Questions

4×2=8

- a) Solve $y = 2px + p^4x^2$.
- b) Reduce the equation $(px - y)(x - yp) = 2p$ to clairuts form by using substitutions $x^2 = u$ and $y^2 = v$ and then solve.
- c) Show that the family of parabolas $y^2 = 4a(x + a)$ is self orthogonal.

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Second Internal Assessment Feb-2024

Sem: V Sub: Real Analysis – II and Complex Analysis Code: 21BSC5C5MATMJ1L

Date: 12 - 02 - 2024

Time: 3:00 PM - 4:00 PM

Max. Marks: 30

Q.No.1. Answer any three of the following. **2×3=6**

- a) State Fundamental theorem of integral calculus.
- b) Evaluate $\int_0^1 x^8(1-x)^7$.
- c) Define harmonic function with an example.
- d) Define bilinear transformation.

Q.No.2. Answer any three of the following. **4×3=12**

- a) If $f(x)$ and $g(x)$ are bounded and R-integrable in $[a, b]$, then prove that $f(x)g(x)$ is R-integrable in $[a, b]$.
- b) Using first mean value theorem prove that $\int_0^\pi \frac{x^2}{5+3\cos x} dx$ lies between $\frac{\pi^3}{24}$ and $\frac{\pi^3}{6}$.
- c) State and prove Abel's test for the convergence of an improper integral.
- d) Prove that $\int_0^1 x^{m-1}(1-x)^{n-1} dx = 2 \int_0^{\frac{\pi}{2}} \sin^{2m-1} x \cos^{2n-1} x dx$.

Q.No.3. Answer any three of the following. **4×3=12**

- a) Prove that an analytic function with constant modulus is constant.
- b) Find the analytic function where $u = x^3 - 3xy^2 + 3x^2 - 3y^2 + 1$
- c) Find the bilinear transformation which maps $z = 1, i, -1$ into $w = i, 0, -i$.
- d) Discuss the transformation $w = e^z$.

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DEPARTMENT OF MATHEMATICS

Second Internal Assessment Feb-2024

Sem: V

Sub: Vector Integration and Analytical
Geometry

Code: 21BSC5C5MATMJ2L

Date: 13 - 02 - 2024

Time: 12:00 Noon - 1:00 PM

Max. Marks: 30

Q.No.1. Answer any three of the following.

2×3=6

- a) Define Curl of a vector function.
- b) State Stokes theorem.
- c) Prove that $\nabla \cdot \nabla \phi = \nabla^2 \phi$.
- d) Show that the planes $2x - 4y + 3z + 5 = 0$ and $10x + 11y + 8z - 17 = 0$ are perpendicular.

Q.No.2. Answer any three of the following.

4×3=12

- a) If a vector function \vec{F} has a continuous second order partial derivate, then prove that $\nabla (\nabla \times \vec{F}) = 0$.
- b) If $\phi = x^3 + y^3 + z^3 - 3xyz$, then find i) $\text{div}(\text{grad } \phi)$ ii) $\text{curl}(\text{grad } \phi)$.
- c) State and prove Gauss divergence theorem.
- d) Evaluate $\iint_S F \cdot \hat{n} ds$ where $F = zi + xj - 3y^2zk$ and S is the surface of the cylinder $x^2 + y^2 = 16$ included in the first octant between $z = 0$ and $z = 5$.

Q.No.3. Answer any three of the following.

4×3=12

- a) Find the equation of the plane that bisects the acute angle between the plane $3x - 6y - 2z + 5 = 0$ and $4x - 12y = 3z - 3 = 0$.
- b) Prove the general equation of first degree in x, y, z represents a plane.
- c) Define enveloping cone and find its equation.
- d) Obtain general form of right circular cylinder.

B.L.D.E.A's

S.B. ARTS AND K.C.P. SCIENCE COLLEGE, VIJAYAPUR-586 103

DEPARTMENT OF MATHEMATICS

First Internal Assessment

Sem: II

Sub: Algebra-II and Calculus-II

Code: 21BSC1C1MAT1L

Date: 11- 07 -2024

Time: 9:30 AM - 10:30 AM

Max. Marks: 30

Q.No.1. Answer Any Three Questions

2×3=6

- a) Define i) Finite set ii) countable set.
- b) If a is any element of group $(G, *)$ then prove that $(a^{-1})^{-1} = a$.
- c) Find $\frac{\partial u}{\partial x}$ and $\frac{\partial u}{\partial y}$ for $u = x^3 + y^3 - 3axy$.
- d) Evaluate $\int_0^1 \int_1^2 (x^2 + y^2) dy dx$.

Q.No.2. Answer Any Three Questions

4×3=12

- a) Prove that every subset of finite set is finite.
- b) Prove that union of countable collection of countable set is countable.
- c) If $G = \{1, 5, 7, 11\}$, then prove that G is abelian group with respective multiplication modulo 12.
- d) i) Define semigroup and give an example.
ii) Prove that the identity element of group $(G, *)$ is unique.

Q.No.3. Answer Any Three Questions

4×3=12

- a) State and prove Euler's theorem for homogeneous function.
- b) If $z = f(x, y)$ where $x = e^u + e^{-v}$ and $y = e^{-u} - e^v$, then show that $\frac{\partial z}{\partial u} - \frac{\partial z}{\partial v} = x \frac{\partial z}{\partial x} - y \frac{\partial z}{\partial y}$.
- c) Evaluate $\int y dx + x dy - z^2 dz$ where c is curve given by $x = \sin t, y = \cos t, z = t^2$ and $0 \leq t \leq 1$.
- d) Evaluate $\int_0^1 \int_0^1 \frac{dx dy}{\sqrt{(1-x^2)(1-y^2)}}$.

B.L.D.E.A's
S.B. ARTS AND K.C.P. SCIENCE COLLEGE, VIJAYAPUR-586 103
DEPARTMENT OF MATHEMATICS
First Internal Assessment July-2024

Sem: IV

Sub: Partial Differential Equations and
Integral Transforms

Code:21BSC4C4MAT2L

Date: 10 - 07 - 2024

Time: 09:30 AM - 10:30 AM

Max. Marks: 30

Q.No.1. Answer any three of the following.

2×3=6

a) Solve $\frac{\partial^2 z}{\partial x^2} + 6 \frac{\partial^2 z}{\partial x \partial y} + 9 \frac{\partial^2 z}{\partial y^2} = 0$.

b) Form the partial differential equation by eliminating arbitrary constant a & b from $z = ax + by + ab$.

c) Find $L[t^3 + 3t^2 - 6t + 8]$.

d) Find a_0 in the fourier series of $f(x) = x + x^2$ and $(-\pi, \pi)$.

Q.No.2. Answer any three of the following.

4×3=12

a) Solve $(D^3 - D^2 D' - 8DD'^2 + 12D'^3)z = 0$.

b) Solve $(D^2 + 2DD' + D'^2)z = e^{2x+3y}$.

c) Derive the partial differential equation of the form $Pp + Qq = R$ by eliminating ϕ from $\phi(u, v) = 0$ where u, v are functions of x, y, z .

d) Solve $(xzp + yzq) = xy$.

Q.No.3. Answer any three of the following.

4×3=12

a) State and prove periodic function.

b) If $L[f(t)] = F(s)$ and $g(t) = \begin{cases} f(t-a) & \text{if } t > a \\ 0 & \text{if } t < a \end{cases}$, then

$L[g(t)] = e^{-as}F(s)$.

c) Obtain the fourier series of $f(x) = x - 1$ when $-\pi < x < \pi$.

d) Obtain the fourier series of $f(x^2)$ where $-\pi < x < \pi$ and

$f(x + 2\pi) = f(x)$ hence deduce that $1 - \frac{1}{4} + \frac{1}{9} - \frac{1}{16} + \dots = \frac{\pi^2}{12}$.

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Sem: VI

Sub: Linear Algebra

Code: 21BSC6C6MATMJ1L

Date: 11 - 07 - 2024

Time: 01:40 PM - 02:40 PM

Max. Marks: 30

Q.No.1. Answer any three of the following.

2×3=6

- a) Define subring and give an example.
- b) Define vector space.
- c) Define Linear Transformation.
- d) Define homomorphism.

Q.No.2. Answer any three of the following.

4×3=12

- a) Prove that a matrix of order 2×2 is a ring.
- b) Prove that a non empty subset S of a ring R is a subring of R iff (i) $a, b \in S \Rightarrow a - b \in S$ (ii) $a, b \in S \Rightarrow ab \in S$.
- c) Show that any field F forms a vector space over itself.
- d) In any vector space V over a field F , then prove that
 - i. $c \cdot 0 = 0 \forall c \in F$.
 - ii. $0 \cdot \alpha = 0 \forall \alpha \in V$.
 - iii. $c \cdot (-\alpha) = -(c\alpha) \forall c \in F, \alpha \in V$.
 - iv. $(-c) \cdot \alpha = -(c\alpha) \forall c \in F, \alpha \in V$.

Q.No.3. Answer any three of the following.

4×3=12

- a) Show that the mapping $T: v_3 \rightarrow v_2$ is defined by $T(x, y, z) = (x - y, x - z)$ is linear transformation.
- b) Let T be a linear transformation from a vector space $u(F)$ into vector space $v(F)$. Then show that
 - i. $T(0) = 0$ where 0 is the Zero vector
 - ii. $T(c_1\alpha_1 + c_2\alpha_2 + \dots + c_n\alpha_n) = c_1 T(\alpha_1) + c_2 T(\alpha_2) + \dots + c_n T(\alpha_n)$
 - iii. $T(-\alpha) = -T(\alpha)$
- c) Prove that every n -dimensional vector space is isomorphic to $V_n(F)$.
- d) If f is a homomorphism of $U(F)$ into $V(F)$, then prove that
 - i. $f(0) = 0'$ where 0 and $0'$ are zero vector of U and V respectively.
 - ii. $f(-\alpha) = -f(\alpha) \forall \alpha \in U$.

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DEPARTMENT OF MATHEMATICS
First Internal Assessment July-2024

Sem: VI

Sub:Numerical Analysis

Code: 21BSC6C6MATMJ2L

Date: 15 - 07 - 2024

Time: 01:40 PM - 02:40 PM

Max. Marks: 30

Q.No.1. Answer any three of the following. 2×3=6

- a) Explain secant method to find the real root of the equation $f(x) = 0$.
- b) Explain the Gauss-Jordan method to solve the system of linear equations.
- c) Write the Newton's forward interpolation formula.
- d) Write the formula to find the first derivative using forward differences.

Q.No.2. Answer any three of the following. 4×3=12

- a) Find the real root of the equation $x^3 - 2x - 5 = 0$ by Regular-False method correct to three decimal places.
- b) Find the real root of the equation $x \log_{10} x = 1.2$ by Newton-Raphson's method correct to three decimal places.
- c) Apply Gauss-Jordan elimination method to solve the system of equations

$$\begin{aligned}x + y + z &= 9 \\x - 2y + 3z &= 8 \\2x + y - z &= 3.\end{aligned}$$

- d) Solve by Triangularization method

$$\begin{aligned}3x + y + 2z &= 16 \\2x - 6y + 8z &= 24 \\5x + 4y - 3z &= 2.\end{aligned}$$

Q.No.3. Answer any three of the following. 4×3=12

- a) Derive Newton's Backward Interpolation formula.
- b) Using forward difference formula, find $f(38)$.

x	40	50	60	70	80	90
f(x)	184	204	226	250	276	304

- c) Find $f'(1.5)$ and $f''(1.5)$ from the following table.

x	1.5	2.0	2.5	3.0	3.5	4.0
f(x)	3.375	7.0	13.62	24.0	38.875	59.0

- d) Find $f'(0.4)$ and $f''(0.4)$ from the following table.

x	0.1	0.2	0.3	0.4
f(x)	1.10517	1.22140	1.34986	1.49182

B.L.D.E.A's
S.B. ARTS AND K.C.P. SCIENCE COLLEGE, VIJAYAPUR-586103
DEPARTMENT OF MATHEMATICS
Second Internal Assessment

Sem: II

Sub: Algebra-II and Calculus-II

Code: 21BSC1C1MAT1L

Date: 05-08-2024

Time: 9:30 AM - 10:30 AM

Max. Marks: 30

Q.No.1. Answer Any Three Questions

2×3=6

- a) Define supremum and infimum of a set.
- b) Prove that every cyclic group is abelian.
- c) Define Jacobian of two variables.
- d) Evaluate $\int_0^1 \int_1^{y^2} e^{x/y} dx dy$.

Q.No.2. Answer Any Three Questions

4×3=12

- a) Prove that the interval $[0,1]$ is uncountable.
- b) State and prove Archimedean property of \mathbb{R} .
- c) Show that the group $(\mathbb{Z}_5, +_5)$ is a cyclic group and every non zero elements of \mathbb{Z}_5 is a generator.
- d) A non empty subset H of a group $(G, *)$ is a subgroup of G iff
 - 1) $\forall a, b \in H = a * b \in H$
 - 2) $\forall a \in H = a^{-1} \in H$.

Q.No.3. Answer Any Three Questions

4×3=12

- a) If $J = \frac{\partial(u,v)}{\partial(x,y)}$, $J' = \frac{\partial(x,y)}{\partial(u,v)}$ then prove that $JJ'=1$.
- b) Expand $e^x \cos y$ by Maclaurin series.
- c) Evaluate $\int_0^1 \int_x^{\sqrt{x}} xy \, dx dy$ by changing the order of integration.
- d) Evaluate $\int_0^a \int_0^{\sqrt{a^2-x^2}} y^2 \sqrt{x^2 + y^2} dy dx$ by transforming to the polar coordinate.

B.L.D.E.A's
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DEPARTMENT OF MATHEMATICS
Second Internal Assessment July-2024

Sem: IV

Sub: Partial Differential Equations and
Integral Transforms

Code:21BSC4C4MAT2L

Date: 07 - 08 - 2024

Time: 09:30 AM - 10:30 AM

Max. Marks: 30

Q.No.1. Answer any three of the following.

2×3=6

- a) Classify $\frac{\partial^2 z}{\partial x^2} + 4 \frac{\partial^2 z}{\partial x \partial y} + 4 \frac{\partial^2 z}{\partial y^2} = 0$.
- b) Find the complete integral of $p^2 - q^2 = 1$.
- c) Find the Laplace transform for $L[t \cdot e^{at}]$.
- d) Define finite sine transform for $f(x)$ in $(0, l)$.

Q.No.2. Answer any three of the following.

4×3=12

- a) Reduce the $r + 2s + t = 0$ to canonical form.
- b) Solve one-dimensional heat equation $u_t = c^2 u_{xx}$ by method of separation of variables.
- c) Solve $z = px + qy + 3(pq)^{\frac{1}{3}}$.
- d) Solve $p^3 + q^3 = 3pqz$.

Q.No.3. Answer any three of the following.

4×3=12

- a) If $L[f(t)] = F(s)$ then $L\left[\frac{f(t)}{t}\right] = \int_s^\infty F(s) ds$.
- b) Prove that $L\{U(t - a)\} = \frac{e^{-as}}{s}$
- c) Find the half range sine and cosine series for the function $f(x) = (\pi - x)$ in the interval $(0, \pi)$.
- d) Find fourier finite cosine transforms of $f(x) = 2 - x$ in $(0, 2)$.

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Second Internal Assessment -2024

Sem: VI

Sub: Linear Algebra

Code: 21BSC6C6MATMJ1L

Date: 03 - 08 - 2024

Time: 03:20 PM - 04:20 PM

Max. Marks: 30

Q.No.1. Answer any three of the following.

2×3=6

- a) Define Maximal Ideal and give an example.
- b) Define Linear Combination of vector.
- c) Define Nullity and rank of linear map.
- d) Find the Eigen value of the matrix $= \begin{bmatrix} 5 & 4 \\ 5 & 6 \end{bmatrix}$.

Q.No.2. Answer any three of the following.

4×3=12

- a) State and prove fundamental theorem of Homomorphism of ring.
- b) Define homomorphism of ring R into R' . If $f: R \rightarrow R'$ is homomorphism, then prove that
 - i) $f(0) = 0'$
 - ii) $f(-a) = -f(a) \forall a \in R$ where $0'$ is the identity in R' .
- c) Let V be a vector space over a field F and W be a non empty subset of V , then
 - W is a subspace of V iff $\alpha w_1 + \beta w_2 \in W \forall \alpha, \beta \in F, w_1, w_2 \in W$.
- d) If $V(F)$ is finite dimensional vector space then any two basis of V have the same number of elements.

Q.No.3. Answer any three of the following.

4×3=12

- a) State and prove Rank-Nullity theorem.
- b) Describe explicitly the linear transformation $T: R^2 \rightarrow R^2$, such that $T(2,3) = (4,5)$ and $T(1,0) = (0,0)$.
- c) State and prove fundamental theorem of Homomorphism of vector space.
- d) Find all the Eigen values and corresponding Eigen vectors of the matrix $\begin{bmatrix} 2 & 2 & 1 \\ -4 & 8 & 1 \\ -1 & -2 & 0 \end{bmatrix}$.

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Second Internal Assessment -2024

Sem: VI

Sub: Numerical Analysis

Code: 21BSC6C6MATMJ2L

Date: 07 - 08 - 2024

Time: 03:20 PM - 04:20 PM

Max. Marks: 30

Q.No.1. Answer any three of the following.

2×3=6

- a) Define absolute and relative error.
- b) Solve by Gauss elimination method $3x - 2y = 5$ and $x + 3y = -2$.
- c) Write the Lagrange's interpolation formula.
- d) State trapezoidal rule to evaluate $\int_a^b f(x)dx$.

Q.No.2. Answer any three of the following.

4×3=12

- a) Derive general error formula.
- b) Obtain the approximation of $\log(1+x)$ in the form of second degree polynomial. Hence evaluate $\log(1.2)$ and its maximum truncation error.
- c) Apply Jacobi iteration method to solve $10x + y + z = 12$, $2x + 10y + z = 13$, $2x + 2y + 10z = 14$.
- d) Explain the Gauss-Seidel method to solve the equations $a_1x + b_1y + c_1z = d_1$, $a_2x + b_2y + c_2z = d_2$, $a_3x + b_3y + c_3z = d_3$.

Q.No.3. Answer any three of the following.

4×3=12

- a) Using divide and difference formula find y at $x = 9$.

x	5	7	11	13	17
$y = f(x)$	150	392	1452	2366	5202

- b) Using Lagrange's interpolation formula find y at $x = 10$.

x	5	6	9	11
$y = f(x)$	12	13	14	16

- c) State and prove general quadrature formula for equidistant ordinate.
- d) Evaluate $\int_4^{5.2} \log(x)dx$ by using (i) trapezoidal rule (ii) Simpsons $1/3^{\text{rd}}$ rule (iii) Simpsons $3/8^{\text{th}}$ rule.